

# More LOTOS Operators

## **TERMINATION IN LOTOS**

### **UNSUCCESSFUL TERMINATION: STOP**

**off\_hook ; tone ; dial ; connect ; breakdown ; stop**

### **SUCCESSFUL TERMINATION: EXIT**

**off\_hook ; tone ; dial ; connect ; exit**

*Unsuccessful termination can be specified either explicitly by a stop or implicitly by the result of a deadlock.*

**ENABLE: ">>"**

**$B_1 \gg B_2$**

*This is a sequential composition between two behavior expressions. Note difference w.r.t. the Action Prefix operator ";".*

**example:**

```
off_hook ;  
  (  
    tone ; dial ; exit  
    [> hang_up; stop  
  )  
  >>  
  connect; talk; stop
```

*The connect and talk actions will not occur if the user hangs up.*

*However if connect occurs, disable becomes impossible.*

## Exit Inference Axiom

$$\text{exit} - \delta \rightarrow \text{stop}$$

A process that exits stops, after having produced action  $\delta$ , which can be picked up by other processes, as we shall see.

## Enable Inference Rules: $B_1 \gg B_2$

$$\frac{B_1 - a \rightarrow B_1'}{B_1 \gg B_2 - a \rightarrow B_1' \gg B_2} \quad (\text{continuation of } B_1)$$

$$\frac{B_1 - \delta \rightarrow B_1'}{B_1 \gg B_2 - i \rightarrow B_2} \quad (B_1 \text{ stops and } B_2 \text{ takes over})$$

Note that by execution of enable  $\delta$  action is *internalized*

The  $\delta$  action has effects  
on the parallel composition:

gate  $\delta$  is always included  
in the synchronization set.

Therefore ...

## EXIT AND PARALLEL COMPOSITION

*An exit of a process that is composed in parallel with other processes can be executed only if all processes exit*

*example:*

**( a ; b ; c ; exit**

**|||**

**d ; e ; f ; stop) >> B**

*will not go to B, because the second parallel process cannot exit.*

*However the following example will exit:*

**a ; b ; c ; exit**

**|||**

**( d ; e ; f ; stop [ > exit )**

*because this time, the second behavior can synchronize at any time on exit*

*exit is triggered by the end of the first parallel process*

*any part of the second parallel process will be executed.*

## GENERAL PARALLELISM INFERENCE RULES WITH EXIT

$$\begin{array}{c}
 \mathbf{B}_1 \text{ -a-} \rightarrow \mathbf{B}'_1, \quad \mathbf{B}_2 \text{ -a-} \rightarrow \mathbf{B}'_2 \\
 \hline
 \text{if } a \in \{g_1, \dots, g_n, \delta\} \\
 \mathbf{B}_1 \parallel [g_1, \dots, g_n] \parallel \mathbf{B}_2 \text{ -a-} \rightarrow \mathbf{B}'_1 \parallel [g_1, \dots, g_n] \parallel \mathbf{B}'_2
 \end{array}$$

$$\begin{array}{c}
 \mathbf{B}_1 \text{ -a}_1\text{-} \rightarrow \mathbf{B}'_1 \\
 \hline
 \text{if } a_1 \notin \{g_1, \dots, g_n, \delta\} \\
 \mathbf{B}_1 \parallel [g_1, \dots, g_n] \parallel \mathbf{B}_2 \text{ -a}_1\text{-} \rightarrow \mathbf{B}'_1 \parallel [g_1, \dots, g_n] \parallel \mathbf{B}_2
 \end{array}$$

$$\begin{array}{c}
 \mathbf{B}_2 \text{ -a}_2\text{-} \rightarrow \mathbf{B}'_2 \\
 \hline
 \text{if } a_2 \notin \{g_1, \dots, g_n, \delta\} \\
 \mathbf{B}_1 \parallel [g_1, \dots, g_n] \parallel \mathbf{B}_2 \text{ -a}_2\text{-} \rightarrow \mathbf{B}_1 \parallel [g_1, \dots, g_n] \parallel \mathbf{B}'_2
 \end{array}$$

*$\delta$  is always included in every synchronization set  
i cannot be included, must interleave*

*Normally all processes combined together by a  $[[...]]$  operator will synchro on  $\delta$ .*

*When  $\delta$  is used by  $>>$ , it becomes internal.*

*It can then interleave with actions of other processes involved in more external parallel composition ops.*

The  $\delta$  action also has effects on the disable operator

Additional disable rule:

$$\frac{B_1 - \delta \rightarrow B_1'}{B_1 [ > B_2 - \delta \rightarrow B_1' }$$

i.e. if  $B_1$  offers  $\delta$  then  
 $B_1 [ > B_2$  offers  $\delta$  and then stops  
 this  $\delta$  can trigger  $>>$ ,  $[ >$  disappears

*specification ENABDISAB [a,b,c,d,e] : noexit  
 behavior*

*(a; b; exit [ > c; d; stop) >> e; stop  
 endspec*

Behavior tree:

```

1 a
| 1 b
| | 1 i (enable: exit)
| | | 1 e DEADLOCK
| | | 2 c
| | | 1 d DEADLOCK
| | 2 c
| | 1 d DEADLOCK
2 c
| 1 d DEADLOCK
  
```

## Example with enable and disable

specification ENABDISAB [a,b,c,d,e] : noexit

behavior

```
(a; b; exit >> c; d; stop) [> e; stop
```

endspec

```
* 1 a [5]
* | 1 b [5]
* | | 1 i (enable: exit) [5]
* | | | 1 c [5]
* | | | | 1 d [5]
* | | | | | 1 e [5] DEADLOCK
* | | | | 2 e [5] DEADLOCK
* | | | 2 e [5] DEADLOCK
* | | 2 e [5] DEADLOCK
* | 2 e [5] DEADLOCK
* 2 e [5] DEADLOCK
```

## ENABLE EXPANSION

```
off_hook ;
(
  tone ;
  (
    dial ;
    (
      i(*exit*); connect ; talk ; stop
      []
      hang_up ; stop
    )
    []
    hang_up ; stop
  )
  []
  hang_up ; stop
)
```

**Note:**

*when exit has been executed, hang\_up can no longer take place in this example.*

*Some interesting examples:*

```
a; b; c; exit
||
(a; b; d; stop
  [> c; exit)
```

*this exit is triggered by the availability of a c after a b.*

```
a; b; exit
||
(a; b; d; stop
  [> i; exit)
```

*i can occur at any time (possibly yielding deadlock). However if a b occurs then it is forced to occur, and process will exit.*

```
a; b; c; exit
||
(a; b; d; stop
  [> i; c; exit)
```

*similar.*

```
a; b; exit
|||
exit
```

*this will exit after a b*

## Some syntax

### Basic Syntax (so far...):

**behexpr** = 'stop' | 'exit' | processname  
          | action ';' behexpr | behexpr op behexpr  
**op** =     '[]' | '|[]|' | '>' | '>>'

### *Examples:*

**stop; exit**                   *all syntactically invalid*  
**stop; a; exit**               *because act. pref. joins*  
**exit; a**                      *an action and a behav. expr.*

**stop >> stop**               *all syntactically valid,*  
**stop >> exit**               *although not*  
**exit >> exit**               *semantically*  
**stop >> a; stop**            *meaningful*

**a; b [] c; d**                *invalid: [] is between behav. expr.*  
**a; b; exit [] c; d; exit**    *OK*  
**a; b; exit [] c; d; stop**    *OK*

**(a; b; stop [] c; d; exit); b; c; stop**        *incorrect*  
**(a; b; stop [] c; d; exit) >> b; c; stop**      *OK*

*If P is a process name (ignoring params), the following are legal*

**a; b; P [] c; d; P**  
**(a; b; stop [] c; d; exit) >> P**

**Operator priorities: ';' > '[]' > '|[]|' > '>' > '>>'**  
                    right-to-left otherwise

## **Multiway Synchro and Hiding**

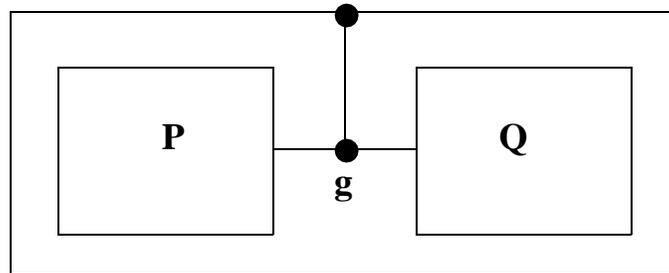
*Following CSP (and unlike CCS) LOTOS adopts a multi-way synchronization concept.*

*In order for an action to be executed, all behaviors that share that action by virtue of the parallel composition operator (and for which the action is not hidden, see later) must simultaneously participate in the action.*

*In CCS, an action becomes internal after it has been used for a two-way synchronization. In LOTOS, the action remains and can cause synchronization of a number of processes. It must be "consumed" in order to disappear. This can be achieved in one of two ways:*

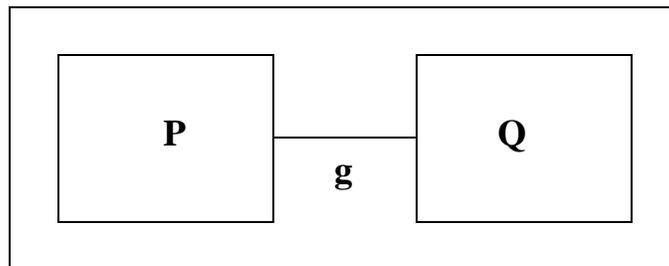
- 1. The action reaches a level where it is 'hidden'*
- 2. If 1 does not happen, the environment must participate in the action*

## HIDING GATES



$P[g] \parallel Q[g]$

requires cooperation of environment on gate  $g$



$\text{hide } g \text{ in } (P[g] \parallel Q[g])$

**P and Q can synchronize on  $g$  without having to synchronize with the environment**

## The HIDE operator

### **hide <gatename> in B**

*In order for an action to be executed, all processes that synchronize on the gate must participate, unless the gate is hidden.*

*1) internalize actions that should not be observable*

```
hide ntwk in  
(  
  phone_one[...]  
  |||  
  phone_two[...]  
)  
  |[ntwk]|  
network[ntwk]
```

*2)*

```
( hide b in  
  
  a ; b ; c ; stop )  
  
  ||  
  
  a ; c ; stop
```

*is equivalent to a; i; c; stop*

3)

*hide c in*

*( c; d; stop*

*//*

*c; d; stop )*

*is equivalent to i; d; stop*

*hidden actions are transformed in internal action i that does not need to synchronize.*

***HIDE ENABLES US TO ABSTRACT  
or INTERNALIZE GATES***

# Hide Inference Rules

$$\frac{B - a \rightarrow B'}{\text{hide } g_1, \dots, g_n \text{ in } B - a \rightarrow \text{hide } g_1, \dots, g_n \text{ in } B'} \quad a \notin \{g_1, \dots, g_n\}$$

$$\frac{B - a \rightarrow B'}{\text{hide } g_1, \dots, g_n \text{ in } B - i \rightarrow \text{hide } g_1, \dots, g_n \text{ in } B'} \quad a \in \{g_1, \dots, g_n\}$$

**Examples:**

**(hide a in a; stop |[a]| a; stop) |[a]| a; stop**

*the first two a synchronize, however the resulting a is transformed in internal action -> the third a causes deadlock*

**hide b in (a; stop |[a]| a; stop) |[a]| a; stop**

*all three a synchronize*

# PROCESS DEFINITION

**PROCESS <name>[gate\_list]: functionality :=**

**..... behavior expression**

**endproc**

*example:*

**process phone[offhook, tone, dial, talk]: exit:=**

**offhook ; tone ; dial ; talk ; exit**

**endproc**

A process has functionality *exit* if it can exit, it has functionality *noexit* otherwise (the precise definition is a bit complicated)..

All gates that appear in a process and are not hidden must appear in the process's parm list.

# PROCESS INSTANTIATION

(inference rules for relabelling)

A sequence of action prefixes can be terminated not only by a **stop** or **exit**, but also by a *process instantiation*.

Suppose that we have            process  $P[g_1, \dots, g_n]$   
and an instantiation                 $P[h_1, \dots, h_n]$

if process  $P[g_1, \dots, g_n]$  can execute action  $g_i$   
then             $P[h_1, \dots, h_n]$  can execute action  $h_i$  .

Note:

This means replacement of gate names at execution time and not at instantiation time.

The shape of the behavior tree cannot be changed by instantiation/relabelling.

## RECURSION

*A sequence of action prefixes can be terminated by a stop or an exit, or also by a process instantiation. Thus, recursion is possible.*

**direct recursion:**

```
process P1 [a, b, c]: noexit:=  
    a ; b ; c ; P1[a, b, c]  
endproc
```

*will generate the following sequence:*

**a ; b ; c ; a ; b ; c ; .....**

**indirect or cross recursion:**

```
process P1 [a, b, c]:noexit:=  
    a ; b ; c ; P2[a, b, c]  
endproc
```

```
process P2 [x, y, z]:noexit:=  
    x ; y ; z ; P1[x, y, z]  
endproc
```

*Instantiating P1[a, b, c] will produce the following sequence:*

**a ; b ; c ; a ; b ; c ; a ; b ; c ; .....**

*This is because of the relabelling [a/x, b/y, c/z]*

**Note also: a; P1[a,b,c]; P2[a, b, c]      SYNTAX ERROR**

**Although rarely done in practice,  
it is possible to exchange gate parameters**

```
process buffer [ in, out ];  
    in;  
    buffer [ out, in ]  
endproc
```

**in; out; in; out; ...**

**Interestingly, such “exchanges” can always be removed**

```
process buffer [ in, out ];  
    in; out;  
    buffer [in, out];  
endproc
```

Recursion makes it possible to define processes that cannot be described as Finite State Machines, e.g.

$$P := a; P [> b; \text{stop}]$$

One way to understand such processes is to apply replacement:

$$P := a; P [> b; \text{stop}]$$
$$a; (a; P [> b; \text{stop}]) [> b; \text{stop}]$$
$$a; (a; (a; P [> b; \text{stop}]) [> b; \text{stop}]) [> b; \text{stop}]$$
$$a; (a; (a; (a; P [> b; \text{stop}]) [> b; \text{stop}]) [> b; \text{stop}]) [> b; \text{stop}]$$

...

which implies that P can synchronize with processes offering the following sequences of actions:

b

a b

a a b

a a a b

a a a a b

... (these are caused by the last disable)

a b b

a a b b

... (these are caused by the 2nd from last disable)

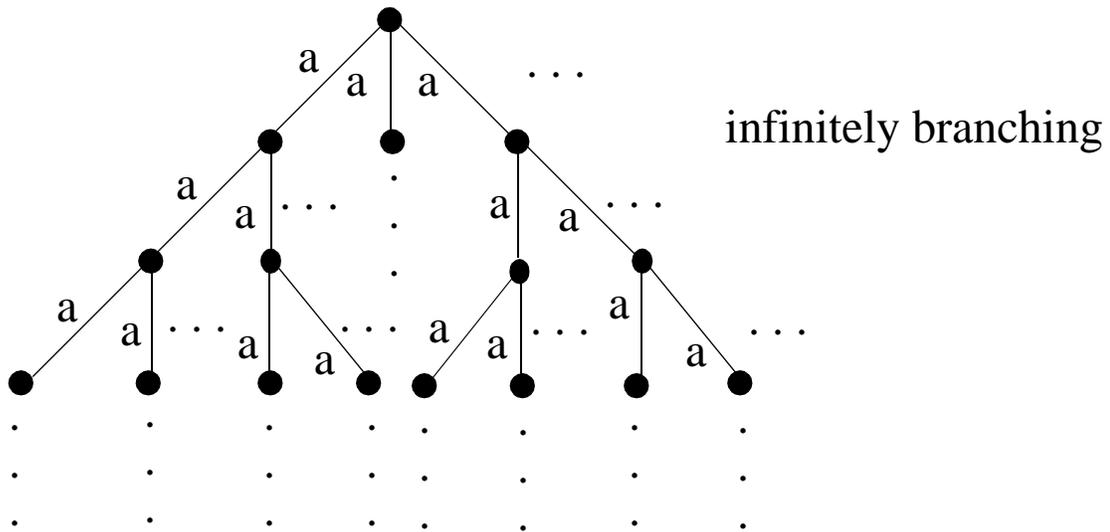
in terms of formal language theory, the *language* of P can be described as

$$a^n b^m \text{ where } n+1 \geq m$$

Note also that this example shows that it may not be possible to redefine a process defined using [> by using only []

Unfortunately, with recursion, it is possible that inference rules will not terminate on legal processes

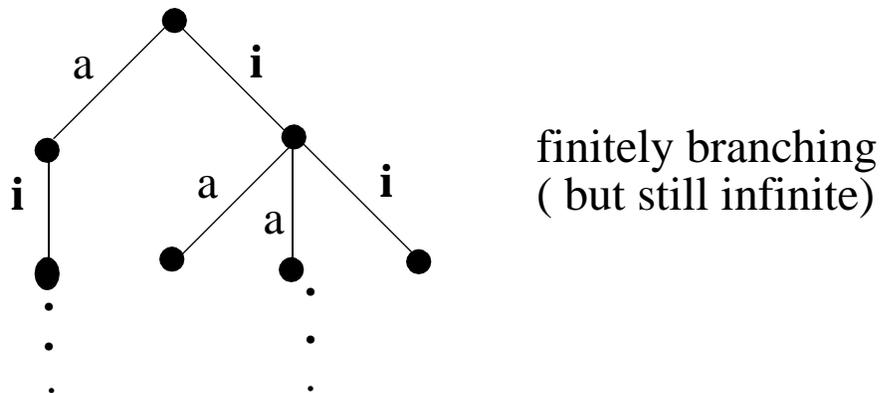
$$P := a ; \mathbf{stop} \parallel \parallel P = P := a ; \mathbf{stop} \parallel a ; \mathbf{stop} \parallel \dots$$



This specific pitfall can be avoided by insisting that recursion be always *guarded*

e.g.

$$P := a ; \mathbf{stop} \parallel \parallel \mathbf{i} ; P$$



**This example shows a common pitfall in LOTOS: since process instantiation is not an action, nor a state in the LTS, in the case of ‘unguarded recursion’, finding the next action may require an infinite number of recursive instantiations, hence the derivation process becomes infinite.**

**Another similar example is:**

$$P := a; \text{stop} [] P$$

**Internal actions stop the derivation process:**

$$P := a; \text{stop} [] i; P$$

# Time-bomb process!

Keep\_out := Time [> Bomb

Time := tick; Time

Bomb := boom; **stop** ||| Bomb

*If you want to include an escape...*

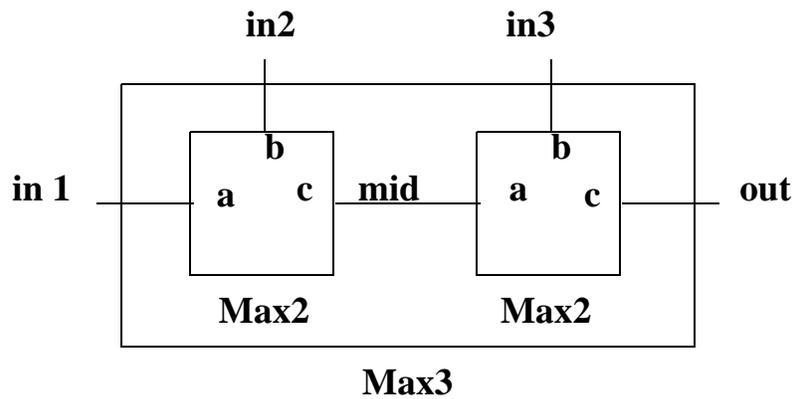
Keep\_out := (Time [> Bomb) >> Run

Time := tick; Time [] **exit**

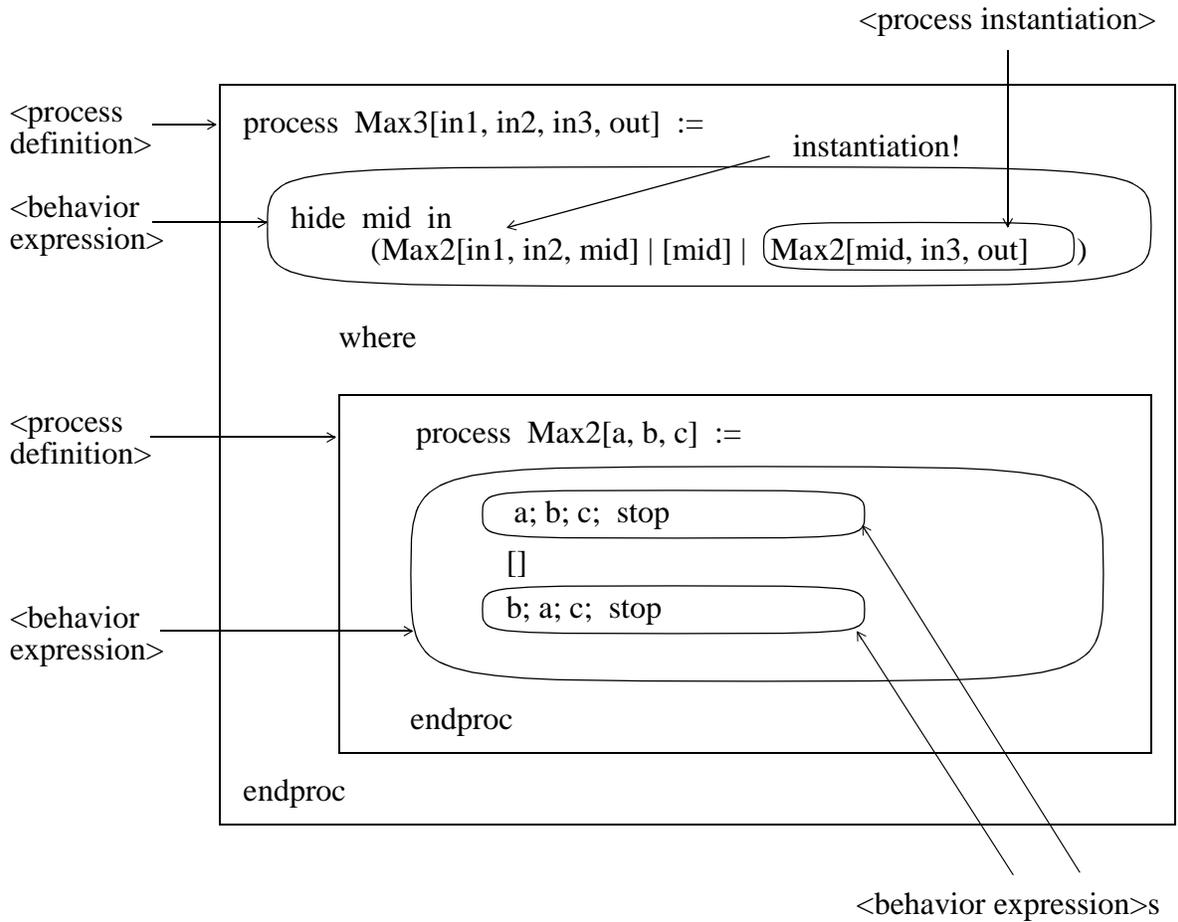
Bomb := boom; **stop** ||| Bomb

Run := run; Run [] **stop**

Infinite recursion impedes finite evaluation and can be prevented by always *guarding* (by any action, even internal) every process instantiation.



Spatial representation of process Max3 (Bolognesi + Brinksma)



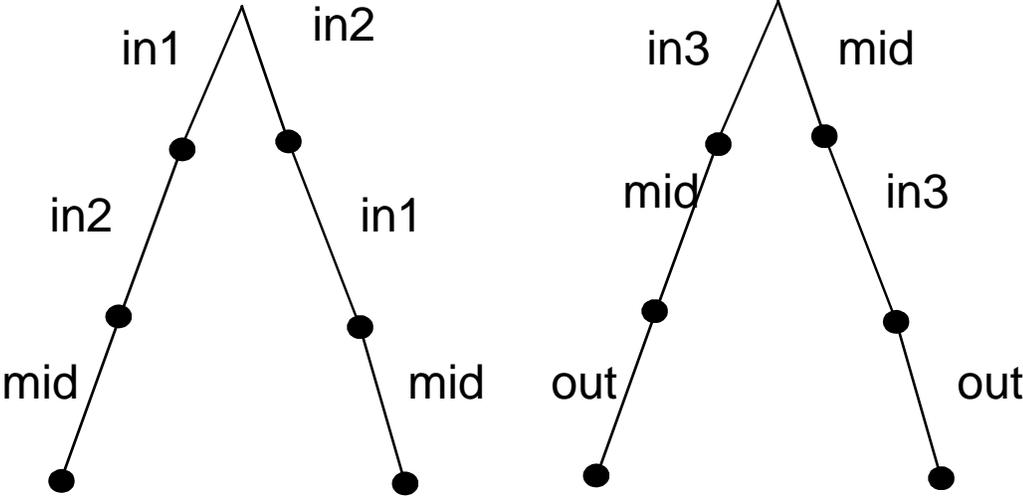
Definition of process Max3

```
process Max2[a, b, c] :=  
  a; b; c; stop  
  []  
  b; a; c; stop  
endproc
```

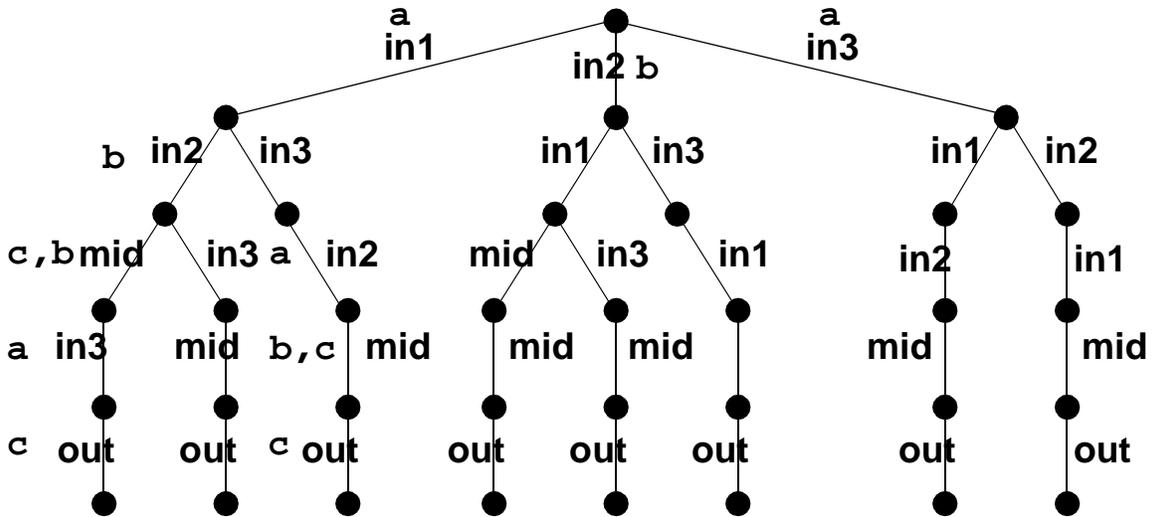
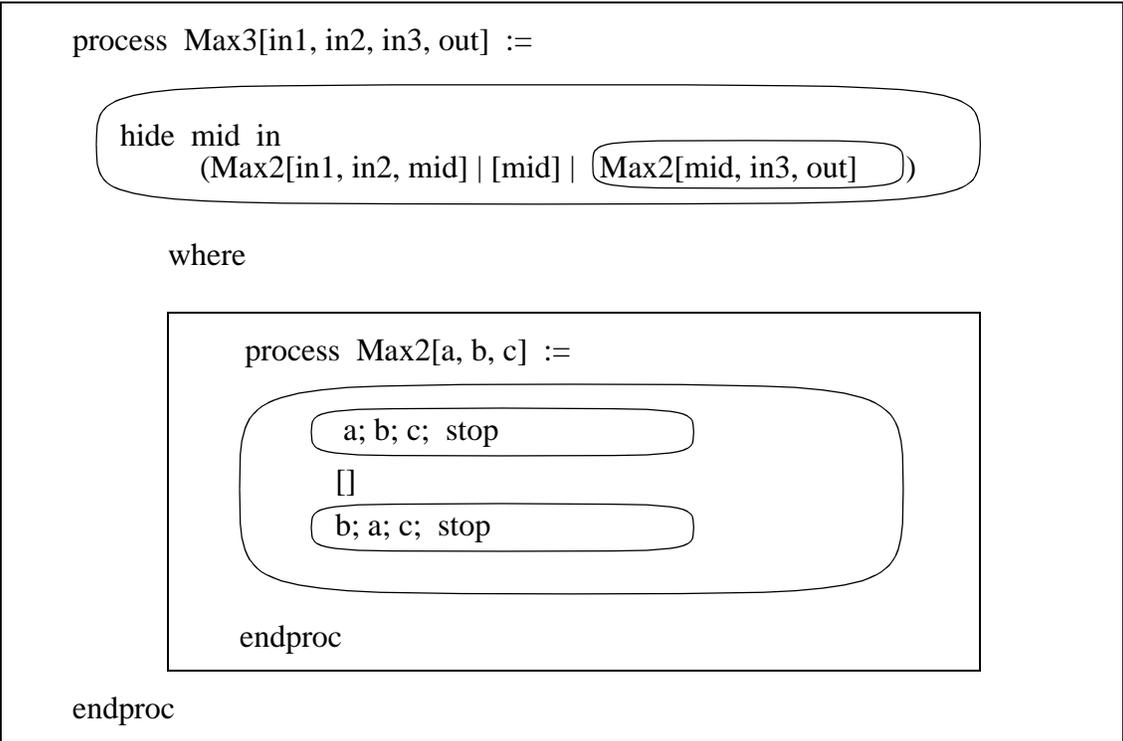
instantiations:

Max2[in1, in2, mid]

Max2[in3, mid, out]



The two behavior trees



# Ken Turner's LIFE Specification

```
1 (* Ken Turner's "Life" specification *)
2
3 specification LIFE
4   [birth, puberty, death, marriage, children]: exit
5 behavior
6
7   BIOLOGY [birth, puberty, death]
8   |[puberty, death]|
9   FAMILY [puberty, marriage, children, death]
10
11 where
12
13   process BIOLOGY [birth, puberty, death]: exit :=
14     birth; ((puberty; stop) [> (death; exit)])
15   endproc
16
17   process FAMILY
18     [puberty, marriage, children, death] : exit :=
19     (
20       puberty; ((marriage; exit) [] exit)
21       |[puberty]|
22       puberty; ((children; exit) [] exit)
23     )
24     |[marriage]|
25     (( marriage; stop) [> (death; exit )])
26   endproc
27
28 endspec
```

## Behavior tree of LIFE specification

```
1 birth [14]
| 1 puberty [14,20,22]
| | 1 children [22]
| | | 1 marriage [20,25]
| | | | 1 death [14,25]
| | | | | 1 exit ** EXIT SUCCEED ** [14,20,22,25]
| | | | 2 death [14,25]
| | | | 1 exit ** EXIT SUCCEED ** [14,20,22,25]
| | 2 marriage [20,25]
| | | 1 children [22]
| | | | 1 death [14,25]
| | | | | 1 exit ** EXIT SUCCEED ** [14,20,22,25]
| | | | 2 death [14,25]
| | | | 1 children [22]
| | | | | 1 exit ** EXIT SUCCEED ** [14,20,22,25]
| | | | 2 exit ** EXIT SUCCEED ** [14,20,22,25]
| | 3 death [14,25]
| | | 1 children [22]
| | | | 1 exit ** EXIT SUCCEED ** [14,20,22,25]
| | | 2 exit ** EXIT SUCCEED ** [14,20,22,25]
| 2 death [14,25] DEADLOCK
```

# RELABELLING

difference with substitution

example:

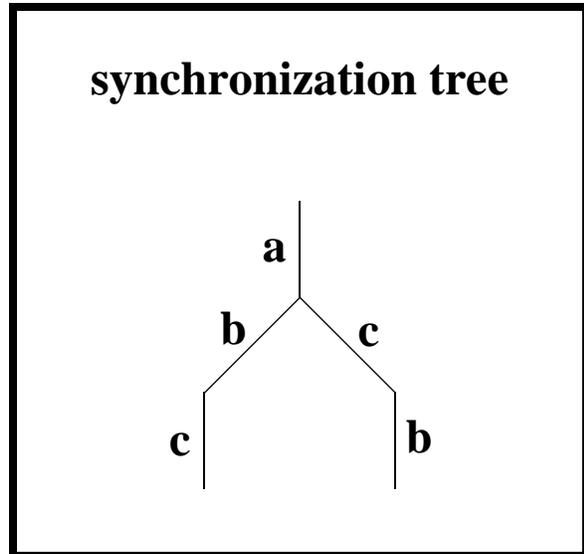
process  $P[a,b,c] :=$

$a ; b ; stop$

$[[a]]$

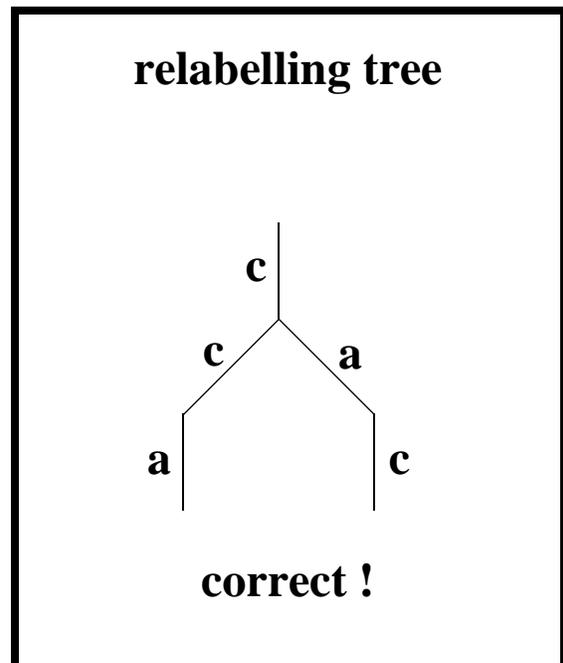
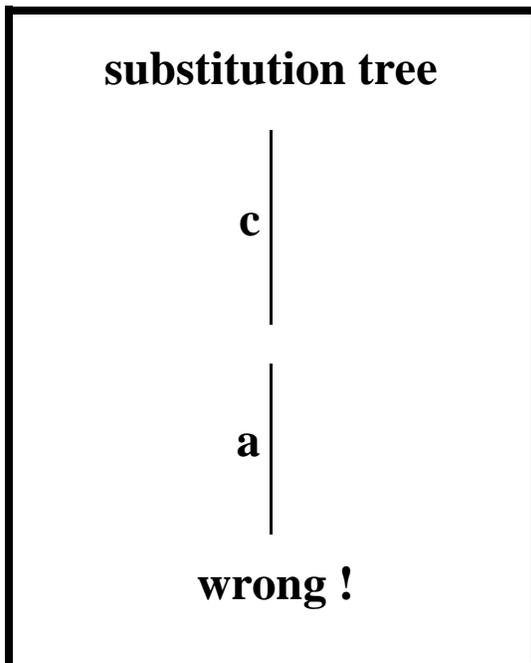
$a ; c ; stop$

endproc



*The principle is: create the synchronization tree first and then relabel its actions.*

*After instantiating with  $P[c,c,a]$*



*note the significant differences in resulting trees*

**Note however:**

*This difference between substitution and relabelling is observable only for gate mappings (formal  $\leftrightarrow$  actual) that are not one-to-one.*

*Most mappings used in practice are one-to-one, so the difference cannot be observed.*

```

1 (* Example to show effect of different gate parameterization
*)
2
3
4 specification gates [a,b,c]: noexit
5
6 behavior
7
8 p[a,b,c]      (* p[a,b,a] *)
9
10 where
11
12     process p[a,b,c]: noexit:=
13         q[a,b] |[a]| r[a,c]
14     endproc
15
16     process q[a,b]: noexit:=
17         a; b; stop
18     endproc
19
20     process r[a,c]: noexit:=
21         c; a; stop
22     endproc
23
24 endspec
25

```

(\* as written \*)

```

bh0 * 1 c line(s): [21]
bh1 * | 1 a line(s): [17,21]
bh2 * | | 1 b line(s): [17] DEADLOCK

```

(\* changing line 8 to p[a,b,a] \*)

```

bh0 * 1 a line(s): [21]
bh1 * | 1 a line(s): [17,21]
bh2 * | | 1 b line(s): [17] DEADLOCK

```

~

## Example with gate parms and hiding

```
process vending_machine [ coin, candy1, candy2 ] :=
  coin;
  ( candy1; vending_machine [coin, candy1, candy2]
    [ ]
    candy2; vending_machine [coin, candy1, candy2] )
endproc
```

```
process devil [ candy ] :=
  candy;
  devil [candy]
endproc
```

```
process system [ coin, candy ] :=
  hide candy_bar in
    ( vending_machine [coin, candy, candy_bar]
      | [ candy_bar ] |
      devil [candy_bar] )
endproc
```

$\approx$

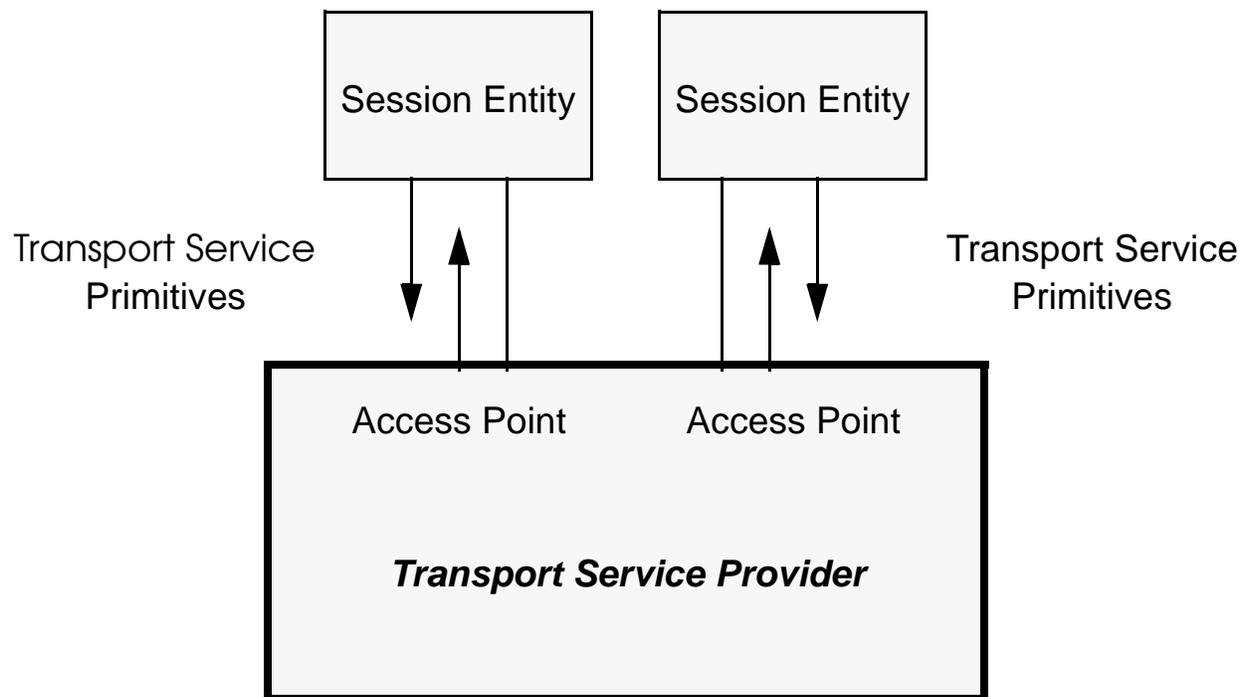
```
process system [coin, candy] :=
  coin; ( candy; system [coin, candy]
    [ ]
    ( i ; system [coin, candy]
      )
  )
endproc
```

*The exact meaning of  $\approx$  is to be discussed.*

**An almost realistic  
example in Basic LOTOS:**

**OSI Transport Service  
Provider**

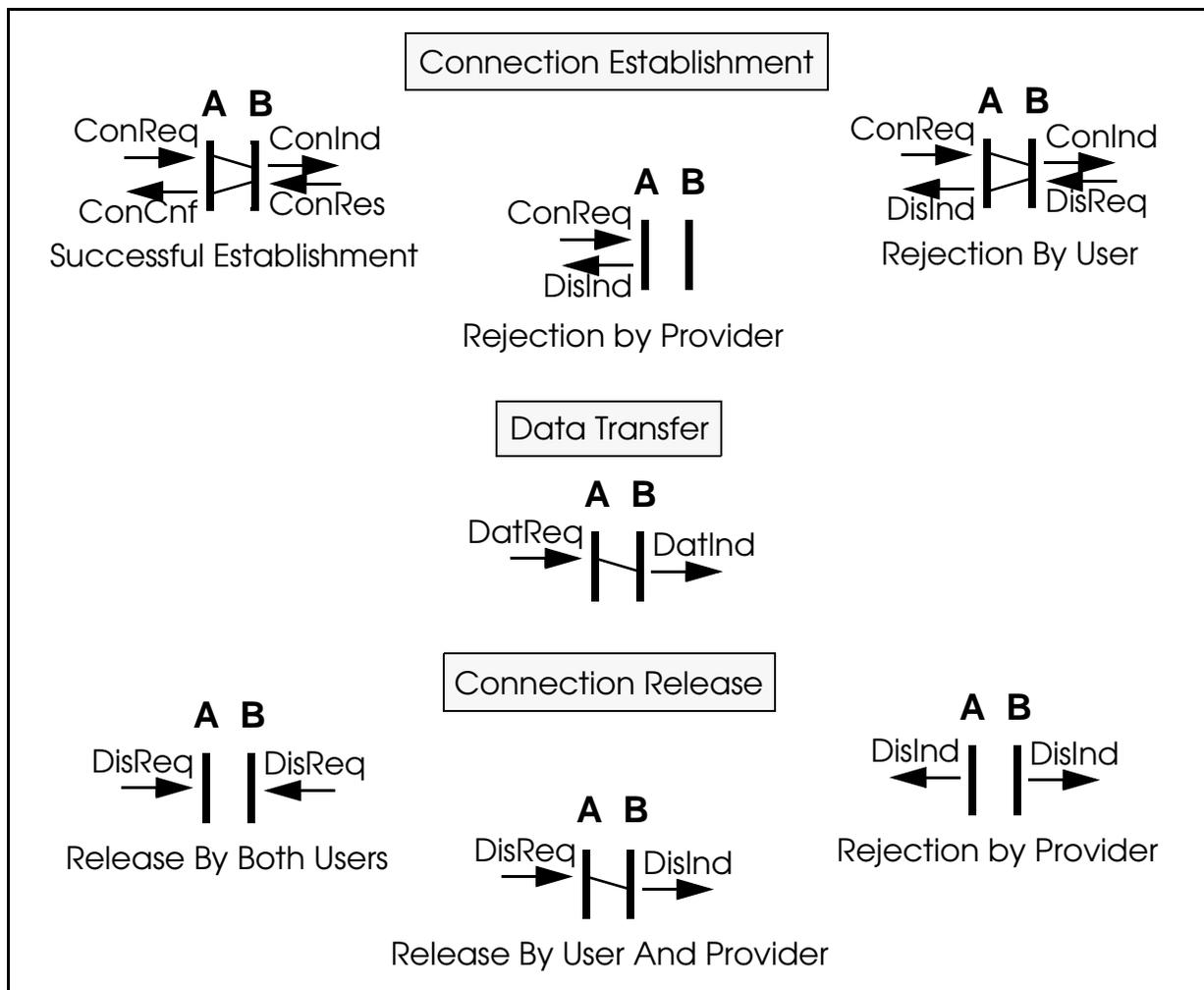
**(from paper by Bolognesi and Brinksma)**



The following table describes the service primitives considered and their significance:

Primitives	Significance
<i>ConReq</i>	Connection Request
<i>ConInd</i>	Connection Indication
<i>ConRes</i>	Connection Response
<i>ConCnf</i>	Connection Confirmation
<i>DisReq</i>	Disconnection Request
<i>DisInd</i>	Disconnection Indication
<i>DatReq</i>	Data Request
<i>DatInd</i>	Data Indication

The service primitive sequences are expressed by Message Sequence Charts:



Process	Phase	Primitives involved
<i>Connection-Phase</i>	<b>Connection establishment</b>	<i>ConReq, ConInd, ConRes, ConCnf, DisReq, DisInd</i>
<i>Data_phase</i>	<b>Data Transfer</b>	<i>DatReq, DatInd</i>
<i>Termination_phase</i>	<b>Connection release</b>	<i>DisReq, DisInd</i>

The main behaviour of the specification can then be written as a call to process *Handler*:

*Handler[ConReq, ConInd, ConRes, ConCnf, DatReq, DatInd, DisReq, DisInd]*

where process *Handler* is defined as follows:

*Connection\_Phase[ConReq, ConInd, ConRes, ConCnf, DisReq, DisInd]*

>>

*(Data\_phase[DatReq, DatInd]*

[>

*Termination\_phase[DisReq, DisInd])*

>>

*Handler[ConReq, ConInd, ConRes, ConCnf, DatReq, DatInd, DisReq, DisInd]*

*Data\_phase* is only enabled when process *Connection\_Phase* terminates successfully. On the other hand, process *Termination\_phase* can disrupt process *Data\_phase* at any time before it terminates. Once process *Termination\_phase* exits, it enables recursively the whole service again by calling process *Handler*.

**process** Handler[ConReq, ConInd, ConRes, ConCnf, DatReq, DatInd, DisReq, DisInd]:=

```
    Connection_Phase[ConReq, ConInd, ConRes, ConCnf, DisReq, DisInd]
  >> (    Data_phase[DatReq, DatInd]
        [>    Termination_phase[DisReq, DisInd]
        )
  >>    Handler[ConReq, ConInd, ConRes, ConCnf, DatReq, DatInd, DisReq, DisInd]
```

**where**

**process** Connection\_Phase[CRq, CI, CR, CC, DR, DI] :=

```
    (    i; Calling[Rq, CI, CR, CC, DR, DI]
      [] Called[Rq, CI, CR, CC, DR, DI]
    )
```

**where**

**process** Calling[Rq, CI, CR, CC, DR, DI]:=

```
    CRq; (    CC; exit
            [] DI; Connection_Phase[CRq, CI, CR, CC, DR, DI]
          )
```

**endproc** (\* Calling \*)

**process** Called[Rq, CI, CR, CC, DR, DI]:=

```
    CI; (    i; CR; exit
           [] i; DR; Connection_Phase[CRq, CI, CR, CC, DR, DI]
         )
```

**endproc** (\* Called \*)

**endproc** (\* Connection\_Phase \*)

**process** Data\_phase[DtR, DtI]

```
    i; DtR; Data_phase[DtR, DtI]
  [] DtI; Data_phase[DtR, DtI]
```

**endproc** (\* Data\_phase \*)

**process** Termination\_phase[DR, DI] :=

```
    i; DR; exit
  [] DI; exit
```

**endproc** (\* Termination\_phase \*)

**endproc** (\* Handler \*)

## Concepts discussed in Class 3:

- termination: exit and stop
- exit and enable
- exit, enable, disable, and par. composition
- hiding and abstraction
- process definition and instantiation
- gate relabeling
- recursion
- pitfalls of unguarded process instantiation
- instantiation, relabeling and parallelism
- the transport service provider in basic LOTOS